

Answers [4 Mark Question]

1) a) $c = 60^\circ$ b) $\cos^{-1}(5/6)$ c) 90° d) $-77/2$ e) i) 22 ii) $\sqrt{145}$ f) 8

2) a) $2^{1/3} \operatorname{cis}\left(\frac{12n\pi - \pi}{18}\right)$ b) $(\sqrt{2})^{1/3} \operatorname{cis}\left(\frac{8n\pi + 3\pi}{12}\right)$

c) $\operatorname{cis}\left(\frac{6n\pi - \pi}{9}\right)$ d) $(2\sqrt{2})^{1/3} \operatorname{cis}\left(\frac{8n\pi + 3\pi}{12}\right)$

e) $2 \operatorname{cis}\left(\frac{12n\pi - 5\pi}{18}\right)$

Here $n=0,1,2,$

3) a) $2^{1/4} \operatorname{cis}\left(\frac{12n\pi - \pi}{24}\right)$ b) $(\sqrt{2})^{1/4} \operatorname{cis}\left(\frac{8n\pi + 3\pi}{16}\right)$

c) $2^{1/4} \operatorname{cis}\left(\frac{6n\pi + \pi}{12}\right)$ d) $\sqrt{2} \operatorname{cis}\left(\frac{4n\pi - \pi}{8}\right)$

Here $n= 0,1,2,3$

4) a) $2^{1/3} \operatorname{cis}\left(\frac{12n\pi + 5\pi}{18}\right),$ Continued Product = $-\sqrt{3} + i$

b) $(\sqrt{2})^{1/3} \operatorname{cis}\left(\frac{8n\pi - 5\pi}{12}\right),$ Continued Product = $1 - i$

c) $4^{1/3} \operatorname{cis}\left(\frac{6n\pi - 2\pi}{9}\right),$ Continued Product = $-2 - 2\sqrt{3}i$

Here : $n= 0,1,2$

5) a) $(\sqrt{2})^{1/4} \operatorname{cis}\left(\frac{8n\pi - 5\pi}{16}\right),$ Continued Product = $1 + i$

b) $4^{1/4} \operatorname{cis}\left(\frac{6n\pi - \pi}{12}\right),$ Continued Product = $-2 + 2\sqrt{3}i$

$$c) 2^{\frac{1}{4}} \operatorname{cis} \left(\frac{12n\pi + 5\pi}{24} \right),$$

$$\text{Continued Product} = \sqrt{3} - i$$

$$d) \operatorname{cis} \left(\frac{6n\pi + 2\pi}{12} \right),$$

$$\text{Continued Product} = \frac{1}{2} - i \frac{\sqrt{3}}{2}$$

Here $n = 0, 1, 2, 3$

$$6) \text{ a) } \sqrt{2} \quad \text{b) } 3\sqrt{2} \quad \text{c) } \frac{21}{\sqrt{26}}$$

7)

$$a) \frac{1}{a} \left[-\cos ax + \frac{\cos^3 ax}{3} \right]$$

$$b) \frac{1}{a} \left[\sin ax - \frac{\sin^3 ax}{3} \right]$$

$$c) \frac{1}{a} \left[\frac{\tan^2 ax}{2} - \log_e(\sec ax) \right]$$

$$d) \frac{1}{a} \left[-\frac{\cot^2 ax}{2} - \log_e(\sin x) \right]$$

$$e) \frac{1}{2a} \left[\tan ax \sec ax + \log_e(\sec ax + \tan ax) \right]$$

$$f) \frac{1}{2a} \left[-\operatorname{cosec} ax \cot ax + \log_e(\operatorname{cosec} ax - \cot ax) \right]$$

$$g) \frac{1}{a} \left[\frac{3ax}{8} + \frac{\sin 4ax}{32} - \frac{\sin 2ax}{4} \right]$$

$$h) \left[\frac{1}{a} \frac{3ax}{8} + \frac{\sin 4ax}{32} + \frac{\sin 2ax}{4} \right]$$

$$i) \frac{1}{a} \left[\frac{\tan^3 ax}{3} + \tan ax + ax \right]$$

$$j) \frac{1}{a} \left[\frac{\cot^3 ax}{3} + \cot ax + ax \right]$$

$$k) \frac{1}{a} \left[\tan ax + \frac{\tan^3 ax}{3} \right]$$

$$l) \frac{1}{a} \left[-\cot ax - \frac{\cot^3 ax}{3} \right]$$

$$m) \frac{1}{4} \left[-\cos 4x + \frac{\cos^3 4x}{3} \right]$$

$$n) \frac{1}{5} \left[\tan 5x + \frac{\tan^3 5x}{3} \right]$$

Here add c at the end to all answers

Answers [2 marks Question]

$$1) \text{ a) } 3 \quad \text{b) } 1 \quad \text{c) } 12 \quad \text{d) } 2 \quad \text{e) } 3$$

$$2) \text{ a) } 7 \quad \text{b) } 3 \quad \text{c) } 9$$

$$3) \text{ a) } 11 \quad \text{b) } 2$$

$$5) \text{ a) } x \equiv 4 \pmod{5}, \text{ b) } x \equiv 3 \pmod{9},$$

$$\text{c) } x \equiv 2 \pmod{9}, x \equiv 5 \pmod{9}, x \equiv 8 \pmod{9},$$

$$\text{d) } x \equiv 2 \pmod{8}, x \equiv 6 \pmod{8},$$

6) a) $\cot x \log_5 e$ b) $\frac{\cot x}{2} \log_{10} e$ c) $-\frac{\tan x}{2} \log_6 e$

d) $\frac{1}{\tan x} \sec^2 x \log_4 e$ e) $\frac{\operatorname{cosec}^2 x}{2 \cot x} \log_{10} e$

f) $\frac{x+1}{x^2+2x+1} \log_5 e$ g) $\operatorname{Tanh} x \log_6 e$

7) a) $\cos\left(\frac{3\pi x}{180}\right)$ $\frac{3\pi}{180}$ b) $-\sin\left(\frac{\pi x}{90}\right)$ $\frac{\pi}{90}$

c) $\sec^2\left(\frac{5\pi x}{180}\right)$ $\frac{5\pi}{180}$

d) $2 \sin\left(\frac{\pi x}{90}\right) \cdot \cos\left(\frac{\pi x}{90}\right)$ $\frac{\pi}{90}$

e) $2 \cos\left(\frac{\pi a x}{180}\right) \left[\sin\left\{\frac{\pi a x}{180}\right\} \right]$ $\frac{\pi a}{180}$

f) $2 \cot\left(\frac{\pi x}{180}\right) \left[-\operatorname{cosec}^2\left\{\frac{\pi x}{180}\right\} \right]$ $\frac{\pi}{180}$

8) a) 1 b) $\frac{5}{2}$ c) 3 d) $\frac{3}{2}$ e) 1 f) 2

9) a) degree = 2, order = 2

b) degree = 3, order = 2

c) degree = 1, order = 3