

COMPLEX NUMBERS AND GENERAL SOLUTIONS

1. If $i = \sqrt{-1}$ and n is a +ve integer, then $i^n + i^{n+1} + i^{n+2} + i^{n+3} =$
- (a) 1 (b) i (c) i^n (d) 0
2. $\left(\frac{1+i}{1-i}\right)^n = 1$, then $n =$
- (a) 4 (b) 5 (c) 9 (d) 7
3. If ω is a cube root of unity, then $(1 - \omega)(1 - \omega^2)(1 - \omega^4)(1 - \omega^8) =$
- (a) 3 (b) ω (c) 9 (d) 1
4. If $(1 + i)(1 + 2i) \dots \dots (1 + ni) = x + iy$, then the value of $2.5.10 \dots \dots (1 + n^2) =$
- (a) $\frac{\sqrt{x} + \sqrt{y}}{2}$ (b) $\frac{\sqrt{x} + \sqrt{y}}{\sqrt{x} - \sqrt{y}}$ (c) $x^2 + y^2$ (d) $x^2 - y^2$
5. If $x + iy = \sqrt{\frac{a+ib}{c+id}}$, then $(x^2 + y^2)^2 =$
- (a) $\frac{c^2+d^2}{a^2+b^2}$ (b) $\frac{a^2-b^2}{c^2-d^2}$ (c) $\frac{\sqrt{a^2+b^2}}{c^2+d^2}$ (d) $\frac{a^2+b^2}{c^2+d^2}$
6. If $z = 1 + i$, then the multiplicative inverse of z^2 is
- (a) $2i$ (b) $1 - i$ (c) $\frac{i}{2}$ (d) $-\frac{i}{2}$
7. If $a = \cos \theta + i \sin \theta$, then $\frac{1+a}{1-a} =$
- (a) $i \cot \frac{\theta}{2}$ (b) $i \tan \frac{\theta}{2}$ (c) $\cot \frac{\theta}{2}$ (d) $\cot \theta$
8. The modulus and amplitude of $\frac{1+i}{1-i}$ are
- (a) $-1, -\frac{\pi}{2}$ (b) $1, \frac{\pi}{2}$ (c) $\sqrt{2}, \frac{\pi}{3}$ (d) $1, \frac{\pi}{4}$
9. $1, \omega, \omega^2$ are cube roots of unity, then their product is
- (a) 1 (b) -1 (c) ω (d) 0
10. In the Argand diagram the points representing the complex numbers $7 + 9i, 3 - 7i$ and $-3 + 3i$
- (a) are collinear (c) form the vertices of an equilateral triangle
- (d) form the vertices of an isosceles triangle (d) from the vertices of a right angled isosceles triangle
11. If we express $\frac{(\cos 2\theta - i \sin 2\theta)^4 (\cos 4\theta + i \sin 4\theta)^{-5}}{(\cos 3\theta + i \sin 3\theta)^{-2} (\cos 3\theta - i \sin 3\theta)^{-9}}$ in the form $x + iy$, we get
- (a) $\cos 21\theta + i \sin 21\theta$ (b) $\cos 49\theta + i \sin 19\theta$ (c) $\cos 23\theta + i \sin 43\theta$ (d) $\cos 49\theta - i \sin 49\theta$
12. Let P be the point represented by the complex number z . Rotate OP (O is the origin) through $\frac{\pi}{2}$ in the anticlock direction, the new position of the complex number is represented by
- (a) $z + i$ (b) iz (c) $z - i$ (d) $\frac{z}{i}$

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13. The value of $\prod_{k=0}^6 \left(\sin \frac{2\pi k}{7} - i \cos \frac{2\pi k}{7} \right)$ is
- (a) 0 (b) i (c) -1 (d) $\frac{z}{i}$
14. If $z(2 - i) = 3 + i$, thus $z^{20} =$
- (a) -1024 (b) $1 - i$ (c) $1 + i$ (d) 1024
15. Let z_1 and z_2 be n th roots of unity which subtend a right angle at the origin. Then n must be of the form
- (a) $4k$ (b) $4k + 3$ (c) $4k + 2$ (d) $4k + 1$
16. The amplitude of $\sin \frac{\pi}{5} + i \left(1 - \cos \frac{\pi}{5} \right)$ is
- (a) $\frac{2\pi}{5}$ (b) $\frac{\pi}{5}$ (c) $\frac{\pi}{15}$ (d) $\frac{\pi}{10}$
17. If $\sqrt{x} + \frac{1}{\sqrt{x}} = 2 \cos \theta$, then $x^6 + x^{-6} =$
- (a) $2 \cos 12\theta$ (b) $2 \cos 6\theta$ (c) $2 \sin 3\theta$ (d) $2 \cos 3\theta$
18. Which of the following is a fourth root of $\frac{1}{2} + i \frac{\sqrt{3}}{2}$?
- (a) $\text{cis } \frac{\pi}{12}$ (b) $\text{cis } \frac{\pi}{2}$ (c) $\text{cis } \frac{\pi}{3}$ (d) $\text{cis } \frac{\pi}{6}$
19. The smallest positive integer n for which $(1 + i)^{2n} = (1 - i)^{2n}$ is
- (a) 1 (b) 2 (c) 3 (d) 4
20. If $\omega = \frac{-1 + \sqrt{3}i}{2}$, then $(3 + \omega + 3\omega^2)^4 =$
- (a) 10 (b) -16 (c) 16ω (d) $16\omega^2$
21. The modulus and amplitude of $\frac{1+2i}{1-(1-i)^2}$ are
- (a) $\sqrt{2}$ and $\frac{\pi}{6}$ (b) 1 and 0 (c) 1 and $\frac{\pi}{3}$ (d) 1 and $\frac{\pi}{4}$
22. The amplitude of $\frac{1+i\sqrt{3}}{\sqrt{3}+i}$ is
- (a) $\frac{\pi}{3}$ (b) $\frac{\pi}{4}$ (c) $\frac{2\pi}{5}$ (d) $\frac{\pi}{6}$
23. The real part of $\frac{1}{1 + \cos \theta + i \sin \theta}$ is
- (a) $-\frac{1}{2}$ (b) $\frac{1}{2}$ (c) $\sqrt{3}$ (d) $\frac{1}{\sqrt{2}}$
24. The complex number $\frac{(-\sqrt{3}+3i)(1-i)}{(3+\sqrt{3}i)(i)(\sqrt{3}+\sqrt{3}i)}$ when represented in the argand diagram is
- (a) In the first quadrant (b) in the second quadrant (c) on the x-axis(Real axis) (d) on the y-axis (Imaginary axis)
25. If $2x = -1 + \sqrt{3}i$, then the value of $(1 - x^2 + x)^6 - (1 - x + x^2)^6 =$
- (a) -64 (b) 32 (c) 0 (d) 64

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26. The modulus and amplitude of $(1 + i\sqrt{3})^8$ are respectively

- (a) 256 and $\frac{2\pi}{3}$ (b) 256 and $\frac{\pi}{3}$ (c) 256 and $\frac{8\pi}{3}$ (d) 2 and $\frac{2\pi}{3}$

27. The real and imaginary part of $\log_e(1 + \sqrt{3}i)$ are

- (a) $\log_e 2$ and $\frac{\pi}{3}$ (b) $\log_e \sqrt{2}$ and $\frac{\pi}{3}$ (c) $\log_e 2$ and $\frac{\pi}{6}$ (d) $\log_e \sqrt{2}$ and $\frac{\pi}{6}$

28. The conjugate of the complex number $\frac{(1+i)^2}{1-i}$ is

- (a) $1 + i$ (b) $1 - i$ (c) $-1 + i$ (d) $-1 + i$

29. The imaginary point of i^i is

- (a) 1 (b) 0 (c) -1 (d) 2

30. The amplitude of $(1 + i)^5$ is

- (a) $-\frac{3\pi}{4}$ (b) $\frac{3\pi}{4}$ (c) $\frac{5\pi}{4}$ (d) $-\frac{5\pi}{4}$

31. If $1, \omega, \omega^2$ are the cube roots of unity, then $(1 + \omega)(1 + \omega^2)(1 + \omega^4)(1 + \omega^8)$ is equal to

- (a) 0 (b) 1 (c) ω (d) ω^2

32. If z is complex number such that $z = -\bar{z}$, then

- (a) Real part of z is the same as its imaginary part (b) z is any complex number
(c) z is purely imaginary (d) z is purely real

33. The maximum value of $|z|$ when z satisfies the condition $\left|z + \frac{2}{z}\right| = 2$ is

- $\sqrt{3} - 1$ (b) $\sqrt{3} + 2$ (c) $\sqrt{3} + 1$ (d) $\sqrt{3}$

34. All complex numbers z which satisfy the equation $\left|\frac{z-6i}{z+6i}\right| = 1$ lie on

- (a) Imaginary axis (b) real axis (c) neither of the axis (d) none of these .

35. The complex number $\frac{1+2i}{1-i}$ lies in

- (a) third quadrant (b) fourth quadrant (c) first quadrant (d) second quadrant

36. If p is the point in the Argand diagram corresponding to the complex number $\sqrt{3} + i$ and if OPQ is an isosceles right angled triangle at 'O', then Q represents the complex number .

- (a) $-1 \pm i\sqrt{3}$ (b) $-1 + i\sqrt{3}$ or $1 - i\sqrt{3}$ (c) $1 \pm i\sqrt{3}$ (d) $\sqrt{3} - i$ or $1 - i\sqrt{3}$

37. The smallest positive integral value 'n' such that $\left(\frac{1 + \sin\frac{\pi}{8} + i \cos\frac{\pi}{8}}{1 + \sin\frac{\pi}{8} - i \cos\frac{\pi}{8}}\right)^n$ is purely imaginary is, n=

- (a) 3 (b) 2 (c) 8 (d) 4

38. The least positive integer n for which $\frac{(1+i)^n}{(1-i)^{n-2}}$ is positive is

- (a) 4 (b) 3 (c) 2 (d) 1

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39. If $x + iy = (-1 + i\sqrt{3})^{2010}$ then x is
 (a) 2^{2010} (b) -2^{2010} (c) 1 (d) -1
40. The value of $\left| \frac{1+i\sqrt{3}}{\left(1+\frac{1}{i+1}\right)^2} \right|$ is
 (a) 20 (b) 9 (c) $\frac{5}{4}$ (d) $\frac{4}{5}$
41. If ω is an imaginary cube root of unity, then the value of $(1 - \omega + \omega^2)(1 - \omega^2 + \omega^8)(1 - \omega^4 + \omega^8) \dots 2n \text{ factors}$ is
 (a) 2^{2n} (b) 2^n (c) 1 (d) 0
42. The conjugate of $\frac{3-2i}{5+7i}$ is
 a. $\frac{1}{74}(1 - 31i)$ b. $\frac{1}{74}(31 + i)$ c. $\frac{1}{74}(31 - i)$ d. $\frac{1}{74}(1 + 31i)$
43. If z_1, z_2, z_3 are complex numbers such that $|z_1| = |z_2| = |z_3| = \left| \frac{1}{z_1} + \frac{1}{z_2} + \frac{1}{z_3} \right| = 1$ then $|z_1 + z_2 + z_3|$ is
 a. 3 b. > 3 c. < 1 d. 1
44. If $i = \sqrt{-1}$, then $4 + 5\left(-\frac{1}{2} + \frac{i\sqrt{3}}{2}\right)^{334} + 3\left(-\frac{1}{2} + \frac{i\sqrt{3}}{2}\right)^{335}$ is equal to
 a. $1 - i\sqrt{3}$ b. $-1 + i\sqrt{3}$ c. $i\sqrt{3}$ d. $-i\sqrt{3}$
45. A point P represents a complex number Z which moves such that $|z - z_1| = |z - z_2|$, then its locus is
 a> a circle with centre at z_1 b> a circle with centre at z
 c> an ellipse d> perpendicular bisector of the line joining z_1 & z_2
46. If $z = cis \left[\frac{\pi}{3^n} \right], n = 1, 2, 3, \dots$ then $z_1 z_2 z_3 \dots$ is
 a. i b. $-i$ c. 1 d. -1
47. If α is a complex number satisfying the equation $\alpha^2 + \alpha + 1 = 0$ then α^{2011} is
 a. α^2 b. α c. $-i$ d. 1
48. If $\omega = cis \frac{2\pi}{3}$, then the value of $\frac{a+b\omega+c\omega^2}{c+a\omega+b\omega^2} + \frac{a+b\omega+c\omega^2}{b+c\omega+a\omega^2}$ is
 a. 0 b. 2 c. 1 d. -1
49. If $|Z^2 - 1| = |Z| + 1$, then Z lies on
 a. an ellipse b. imaginary axis c. circle d. real axis
50. If $|Z| = 1$, then $\frac{1+Z}{1+\bar{Z}}$ is
 a. Z b. \bar{Z} c. 1 d. $Z + \bar{Z}$
51. If Z_1 & Z_2 are two non zero complex numbers such that $|Z_1 + Z_2| = |Z_1| + |Z_2|$ then $arg Z_1 - arg Z_2$ is
 a. 0 b. $\frac{\pi}{2}$ c. π d. $-\frac{\pi}{2}$
52. If $(1 + i)(1 + 2i)(1 + 3i)(1 + 4i) = (i - 1)(i - 2)(i - 3)k$, K is real then $k =$
 a. $\sqrt{17}$ b. $\pm\sqrt{17}$ c. ω d. none
53. Let Z_1 & Z_2 be n th roots of unity which subtends right angle at the origin. Then n must be in the form
 a. $4k + 3$ b. $4k$ c. $4k + 1$ d. $4k + 2$

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68. The value of $\sinh ix$ is
(a) $\sin x$ (b) $i \sin x$ (c) $-i \sin x$ (d) $\sinh x$
69. If the area of triangle formed by z , $z + iz$ & iz is 50, then the value of $|z|$ is
(a) 1 (b) 5 (c) 10 (d) 15
70. If $(x + 2y) + i(2x + y) = 1 + i$ then (x, y) is
(a) (3,3) (b) $\left(-\frac{1}{3}, -\frac{1}{3}\right)$ (c) $\left(\frac{1}{3}, \frac{1}{3}\right)$ (d) (-3, -3)
71. If $\frac{1}{i} + \frac{3}{i^2} + \frac{1}{i^7} + \frac{3}{i^8} = x + iy$, then (x, y) is
(a) (1,1) (b) (i, i) (c) (0,0) (d) (-1, -1)
72. If $x = a - b, y = a\omega - b\omega^2, z = a\omega^2 - b\omega$ then the value of xyz is
(a) 0 (b) $a^3 - b^3$ (c) $a^3 + b^3$ (d) $(a - b)^3$
73. If $\alpha_1, \alpha_2, \alpha_3, \alpha_4, \alpha_5, \alpha_6$ are sixth roots of unity then the value of $(1 + \alpha_1)(1 + \alpha_2)(1 + \alpha_3)(1 + \alpha_4)(1 + \alpha_5)(1 + \alpha_6)$ is
(a) 0 (b) 2 (c) 1 (d) -1
74. If $\alpha_1, \alpha_2, \alpha_3, \alpha_4, \alpha_5$ are fifth roots of unity then the value of $(1 + \alpha_1)(1 + \alpha_2)(1 + \alpha_3)(1 + \alpha_4)(1 + \alpha_5)$ is
(a) 0 (b) 2 (c) 1 (d) -1
75. If α & β are different complex numbers with $|\beta| = 1$, then $\left|\frac{\beta - \alpha}{1 - \bar{\alpha}\beta}\right|$ is equal to
(a) 0 (b) $\frac{1}{2}$ (c) 1 (d) 2
76. If A, B, C, D are angles of a quadrilateral then the values of $\operatorname{cis} A \operatorname{cis} B \operatorname{cis} C \operatorname{cis} D$ is
(a) i (b) $-i$ (c) 1 (d) $1 + i$
77. If $x = \cos \alpha + i \sin \alpha, y = \cos \beta + i \sin \beta, z = \cos \gamma + i \sin \gamma$ and $x^2y + y^2z + z^2x = xyz$, then $\cos(\alpha - \beta) + \cos(\beta - \gamma) + \cos(\gamma - \alpha)$ is
(a) 1 (b) 0 (c) -1 (d) does not exist
78. The real part of $\log(\log i)$ is
(a) $\frac{\pi}{2}$ (b) $\log \frac{\pi}{2}$ (c) 0 (d) does not exist.
79. If $z^4 = i$ then z is
(a) 1 (b) i (c) $\operatorname{cis} \frac{\pi}{4}$ (d) $\operatorname{cis} \frac{\pi}{8}$
80. If ω is an imaginary cube root of unity, then the conjugate of $\frac{1}{1 + \omega}$ is
(a) $1 - \omega$ (b) $1 + \omega$ (c) ω (d) ω^2
81. In any ΔABC , the value of $(e^{iA} e^{iB} e^{iC})^{2012}$ is
(a) 1 (b) -1 (c) 0 (d) $A + B + C$

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82. If $\alpha, \beta, \gamma, \delta$ are the roots of the equation $x^4 - 1 = 0$, then $|1 + \alpha|^{10} + |1 + \beta|^{10} + |1 + \gamma|^{10} + |1 + \delta|^{10}$ is divisible by
 (a) 17 (b) 10 (c) 5 (d) 19
83. The value of $(\cosh x + \sinh x)^n$ is
 (a) $\cosh x + \sinh x$ (b) $\cosh nx + \sinh nx$ (c) $\cosh nx - \sinh nx$ (d) none
84. The value of sum $\sum_{n=1}^{13} (i^n + i^{n+1})$, is
 (a) i (b) $i - 1$ (c) $-i$ (d) 0
85. If n is an odd integer, then $(1 + i)^{6n} + (1 - i)^{6n}$ is equal to
 (a) 0 (b) 2 (c) -2 (d) none of these
86. The value of $\sin^{-1} \left\{ \frac{1}{i}(z - 1) \right\}$, where z is non real, can be the angle of a triangle, if
 (a) $Re(z) = 1, Im(z) = 2$ (b) $Re(z) = 1, -1 \leq y \leq 1$ (c) $Re(z) + Im(z) = 0$ (d) none
87. The $Im(z)$ is equal to
 (a) $\frac{1}{2}(Z + \bar{Z})$ (b) $\frac{1}{2}(Z - \bar{Z})$ (c) $\frac{1}{2}(\bar{Z} - Z)i$ (d) none of these
88. If $z = 1 + i \tan \alpha$, $\pi < \alpha < \frac{3\pi}{2}$, then $|Z|$ is equal to
 (a) $\sec \alpha$ (b) $-\sec \alpha$ (c) $\operatorname{cosec} \alpha$ (d) none of these
89. If $(x - 1)^4 - 16 = 0$, then the sum of non real complex values of x is
 (a) 2 (b) 0 (c) 4 (d) none
90. The value of $\operatorname{amp}(i\omega) + \operatorname{amp}(i\omega^2)$, where ω is a non real cube root of unity is
 (a) 0 (b) $\frac{\pi}{2}$ (c) π (d) $-\frac{\pi}{2}$
91. If α is a non real $\sqrt[5]{1}$, then the value of $2^{|1+\alpha+\alpha^2+\alpha^{-1}+\alpha^{-2}|}$ is equal to
 (a) 4 (b) 2 (c) 1 (d) none
92. If the fourth roots of unity are z_1, z_2, z_3, z_4 , then $z_1^2 + z_2^2 + z_3^2 + z_4^2$ is
 (a) 1 (b) 0 (c) i (d) none
93. $\sqrt{-1 - \sqrt{-1 - \sqrt{-1 - \dots \infty}}}$ is equal to
 (a) ω or ω^2 (b) $-\omega$ or $-\omega^2$ (c) $1 + i$ or $1 - i$ (d) $-1 + i$ or $-1 - i$
94. The inequality $|z - 4| < |z - 2|$ represents the region given by
 (a) $Re(z) > 0$ (b) $Re(z) < 0$ (c) $Re(z) > 2$ (d) $Re(z) > 3$
95. If $|z_1| = |z_2| = |z_3| = |z_4|$, then the points representing z_1, z_2, z_3, z_4
 (a) concyclic (b) vertices of a square (c) vertices of a rhombus (d) none
96. The expression $\tan \left[i \log \left(\frac{a-ib}{a+ib} \right) \right]$ reduces to
 (a) $\frac{ab}{a^2+b^2}$ (b) $\frac{2ab}{a^2-b^2}$ (c) $\frac{ab}{a^2-b^2}$ (d) $\frac{2ab}{a^2+b^2}$

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97. If z is a complex number, then $z^2 + \bar{z}^2 = 2$ represents

- (a) circle (b) parabola (c) hyperbola (d) ellipse

98. If $\begin{vmatrix} 6i & -3i & 1 \\ 4 & 3i & -1 \\ 20 & 3 & i \end{vmatrix} = x + iy$, then

- (a) $x = 0, y = 1$ (b) $x = 1, y = 3$ (c) $x = 0, y = 3$ (d) $x = 0, y = 0$

99. The value of $\left(\frac{1+i}{\sqrt{2}}\right)^8 + \left(\frac{1-i}{\sqrt{2}}\right)^8$ is

- (a) 4 (b) 6 (c) 8 (d) 2

100. If $x + iy = \frac{u+iv}{u-iv}$, then $x^2 + y^2$ is

- (a) 1 (b) -1 (c) 0 (d) none

1. The general solution of $\tan 3x = 1$ is

- (a) $n\pi + \frac{\pi}{4}$ (b) $\frac{n\pi}{3} + \frac{\pi}{12}$ (c) $n\pi$ (d) $n\pi \pm \frac{\pi}{4}$

2. The solution of $\tan 2\theta \tan \theta = 1$ is

- (a) $\frac{\pi}{3}$ (b) $(3n \pm 1)\frac{\pi}{6}$ (c) $(4n \pm 1)\frac{\pi}{6}$ (d) $2n\pi \pm \frac{\pi}{3}$

3. If $\sin x - \cos x = \sqrt{2}$, then $x =$

- (a) $2n\pi$ (b) $n\pi$ (c) $(2n + 1)\pi$ (d) $2n\pi + \frac{3\pi}{4}$

4. If $\sin A = \sin B$ and $\cos A = \cos B$, then

- (a) $A = n\pi + B$ (b) $A = n\pi - B$ (c) $A = 2n\pi + B$ (d) $A = 2n\pi - B$

5. If A and B are acute angles such that $\sin A = \sin^2 B$ and $2\cos^2 A = 3\cos^2 B$, then A is

- (a) $\frac{\pi}{6}$ (b) $\frac{\pi}{4}$ (c) $\frac{\pi}{8}$ (d) $\frac{\pi}{3}$

6. General solution of $\tan 5\theta = \cot 2\theta$ is

- (a) $\theta = \frac{n\pi}{7} + \frac{\pi}{2}$ (b) $\theta = \frac{n\pi}{7} + \frac{\pi}{3}$ (c) $\theta = \frac{n\pi}{7} + \frac{\pi}{14}$ (d) $\theta = \frac{n\pi}{7} - \frac{\pi}{14}$

7. If $\cos \theta = -\frac{1}{2}$ and $0 < \theta < 360^\circ$, then the solutions are

- (a) $\theta = 60^\circ, 240^\circ$ (b) $\theta = 120^\circ, 240^\circ$ (c) $\theta = 120^\circ, 210^\circ$ (d) $\theta = 120^\circ, 300^\circ$

8. The general solution of the equation $\sin \theta + \cos \theta = 1$ is

- (a) $\theta = n\pi + ((-1)^n + 1)\frac{\pi}{4}, n = 0, \pm 1, \pm 2, \dots$ (b) $\theta = 2n\pi, n = 0, \pm 1, \pm 2, \dots$
 (c) $\theta = 2n\pi + \frac{\pi}{2}, n = 0, \pm 1, \pm 2, \dots$ (d) $\theta = n\pi - (1 - (-1)^n)\frac{\pi}{4}, n = 0, \pm 1, \pm 2, \dots$

9. The general solution of the equation $\tan 2\theta \tan \theta = 1$ for $n \in Z$ is $\theta =$

- (a) $(2n + 1)\frac{\pi}{4}$ (b) $(4n + 1)\frac{\pi}{6}$ (c) $(2n + 1)\frac{\pi}{2}$ (d) $(2n + 1)\frac{\pi}{3}$

10. If $0 \leq x \leq \pi$ and $81^{\sin^2 x} + 81^{\cos^2 x} = 30$, then $x =$

- (a) $\frac{\pi}{6}$ (b) $\frac{\pi}{2}$ (c) $\frac{\pi}{4}$ (d) $\frac{3\pi}{4}$

11. The general solution of $\sin x - \cos x = \sqrt{2}$, for any integer n is

- (a) $n\pi$ (b) $2n\pi + \frac{3\pi}{4}$ (c) $2n\pi$ (d) $(2n + 1)\pi$

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12. If $\sin 3\theta = \sin \theta$, how many solutions exist such that $-2\pi < \theta < 2\pi$?
 (a) 9 (b) 8 (c) 7 (d) 4
13. If $1 + \sin x + \sin^2 x + \dots$ upto $\infty = 4 + 2\sqrt{3}$, $0 < x < \pi$ and $x \neq \frac{\pi}{2}$, then $x =$
 (a) $\frac{2\pi}{3}$ (b) $\frac{\pi}{3}$ (c) $\frac{\pi}{6}$ (d) $\frac{\pi}{3}$
14. The general solution of $1 + \sin^2 x = 3 \sin x \cos x$, $\tan x \neq \frac{1}{2}$ is
 (a) $2n\pi - \frac{\pi}{4}$ (b) $2n\pi + \frac{\pi}{4}$ (c) $n\pi + \frac{\pi}{4}$ (d) $n\pi - \frac{\pi}{4}$
15. A value of θ satisfying $\sin 5\theta - \sin 3\theta + \sin \theta = 0$ such that $0 < \theta < \frac{\pi}{2}$
 (a) $\frac{\pi}{12}$ (b) $\frac{\pi}{6}$ (c) $\frac{\pi}{4}$ (d) $\frac{\pi}{2}$
16. The general solution of $\cos x + \sin x = \sqrt{2}$
 (a) $x = 2n\pi + \frac{\pi}{4}$ (b) $2n\pi - \frac{\pi}{4}$ (c) $x = n\pi - \frac{\pi}{4}$ (d) $x = n\pi + \frac{\pi}{4}$
17. If $\log_{10}(1 - \cos x) + \log_{10}(1 + \cos x) = 0$, then $x =$
 a) $\frac{\pi}{3}$ b) $-\frac{\pi}{3}$ c) $\frac{\pi}{2}$ d) $\frac{\pi}{4}$
18. If $x = \cos x$ & $y = \sin 3x$, then x is
 a) $\frac{\pi}{8}$ b) $\frac{\pi}{4}$ c) $\frac{\pi}{2}$ d) π
19. General solution of $\tan \theta + \tan 2\theta + \sqrt{3} \tan \theta \tan 2\theta = \sqrt{3}$ is $\theta =$
 a) $n\pi + \frac{\pi}{3}$ b) $n\pi + \frac{\pi}{6}$ c) $n\pi - \frac{\pi}{3}$ d) $\frac{1}{3}(n\pi + \frac{\pi}{3})$
20. If $\sin 11x \sin 4x + \sin 5x \sin 2x = 0$, then x is
 (a) $\frac{n\pi}{9}$ (b) $\frac{n\pi}{3}$ (c) $\frac{n\pi}{4}$ (d) $\frac{n\pi}{2}$
21. If $\tan \theta + \sec \theta = p$, then θ can be written as
 (a) $\sec^{-1} \left[\frac{1+p^2}{2p} \right]$ (b) $\cos^{-1} \left[\frac{1+p^2}{2p} \right]$ (c) $\tan^{-1} \left[\frac{2p}{p^2-1} \right]$ (d) $\tan^{-1} \frac{p^2-1}{2p}$
22. The general solution of the equation $(2 - \sqrt{3}) \cos \theta - \sin \theta = \sqrt{3} - 1$ is $\theta =$
 a) $2n\pi - 5\frac{\pi}{12}$ b) $2n\pi \pm \frac{\pi}{3} - \frac{5\pi}{12}$ c) $2n\pi \pm \frac{\pi}{4}$ d) $2n\pi \pm \frac{\pi}{4} - \frac{5\pi}{12}$
23. If $0 \leq x \leq \pi$ and $81^{\sin^2 x} + 81^{\cos^2 x} = 30$, then $x =$
 a) $\frac{\pi}{6}$ b) $\frac{\pi}{2}$ c) $\frac{\pi}{4}$ d) $\frac{3\pi}{4}$
24. The general solution of $\sin x + \cos x = k$, where k is the minimum of 1 and $a^2 - 4a + 6$, $a \in R$ is $x =$
 a) $2n\pi$ b) $2n\pi + (-1)^n \frac{\pi}{6}$ c) $2n\pi + (-1)^n \frac{\pi}{4} - \frac{\pi}{4}$ d) $2n\pi + (-1)^n \frac{\pi}{4}$
25. The most general value of θ which satisfies $\sin \theta = -\frac{1}{2}$ & $\tan \theta = \frac{1}{\sqrt{3}}$ is
 a) $2n\pi + \frac{\pi}{6}$ b) $2n\pi + \frac{11\pi}{6}$ c) $2n\pi + \frac{7\pi}{6}$ d) $2n\pi + \frac{\pi}{4}$
26. The equation $\sin x + \sin y + \sin z = -3$ for $0 \leq x \leq 2\pi, 0 \leq y \leq 2\pi, 0 \leq z \leq 2\pi$ has
 a) one solution b) two sets of solution c) four sets of solution d) no solution
27. The number of values of x in the interval $[0, 5\pi]$ satisfying the equation $3\sin^2 x - 7\sin x + 2 = 0$ is
 a) 0 b) 5 c) 10 d) 6

COMPLEX NUMBERS AND GENERAL SOLUTIONS

28. If $1 + \cos x + \cos^2 x + \cos^3 x + \dots = 2 - \sqrt{2}$, then $x(0 < x < \pi)$ is
a) $\frac{3\pi}{4}$ b) $\frac{\pi}{4}$ c) $\frac{\pi}{6}$ d) $\frac{\pi}{8}$
29. The equation $\sin x + \cos x = 2$ has
a) one solution b) infinite many solution c) no solution d) three solution in $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$
30. The number of values of x in the interval $(0, 2\pi)$ such that $4 \sin^2 x = 1$ is
(a) 2 (b) 3 (c) 4 (d) 6
31. If $x = \tan \theta$ and $x + \frac{1}{x} = 2$ then θ is
(a) $\frac{\pi}{4}$ (b) $\frac{3\pi}{4}$ (c) $\frac{5\pi}{4}$ (d) $\frac{\pi}{2}$
32. The equation $e^{\sin x} + e^{-\sin x} + 1 = 0$ has
(a) only one solution (b) infinite solutions (c) no real solutions (d) 3 solutions
33. If $2^{\sin x + \cos y} = 1$, $16^{\sin^2 x + \cos^2 y} = 4$, then $\sin x$ is
(a) $\frac{1}{2}$ (b) $\pm \frac{1}{\sqrt{2}}$ (c) $\pm \frac{\sqrt{3}}{2}$ (d) $\pm \frac{1}{2}$
34. If $2^{1 + \cos^2 x + \cos^4 x + \dots} = 4$ then the value of x are
(a) $\frac{\pi}{4}, -\frac{\pi}{4}$ (b) $\frac{\pi}{6}, -\frac{\pi}{6}$ (c) $\frac{\pi}{3}, -\frac{\pi}{3}$ (d) $\frac{\pi}{2}, -\frac{\pi}{2}$
35. The smallest positive integer satisfying $\log_{\cos x} \sin x + \log_{\sin x} \cos x = 2$ is
(a) $\frac{\pi}{3}$ (b) $\frac{\pi}{2}$ (c) $\frac{\pi}{6}$ (d) $\frac{\pi}{4}$